1 2	JWST Coronagraphic Images of 14 Her c: a Cold Giant Planet in a Dynamically Hot, Multi-planet System
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ABSTRACT

Most observed multi-planet systems are coplanar, in a dynamically "cold" configuration of concentric 23 orbits like our own Solar System. With the James Webb Space Telescope (JWST) we have detected 24 14 Her c, the first mature and cold exoplanet directly imaged in a dynamically "hot", multi-planet 25 system. With large eccentricities and a nonzero mutual inclination, the present-day architecture of this 26 system points to a turbulent past and ongoing angular momentum exchange between the planetary 27 orbits of 14 Her b and c. The temperature of 14 Her c rivals both the coldest imaged exoplanet and 28 the coldest known brown dwarf. Moreover, its photometry at 4.4 µm is consistent with the presence of 29 carbon disequilibrium chemistry and water ice clouds in its atmosphere. 14 Her c presents a unique 30 laboratory to study giant planet formation, dynamical evolution of multi-planet system architectures, 31 and atmospheric composition and dynamics in extremely cold worlds. 32

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Keywords: James Webb Space Telescope (2291), Exoplanets (498), Extrasolar gaseous giant planets (509), Direct imaging (387), Exoplanet atmospheres (487), Exoplanet dynamics (490)

1. INTRODUCTION

The early evolution of our own Solar System was dominated by the dynamical influence of the gas giants (S. N. Raymond 2024). After the dispersal of gas in the protoplanetary disk, Jupiter may have scattered the outer giant planets onto wider orbits, and even possibly prompted the ejection of a fifth giant planet (D. Nesvorný 2011). The final outcome of the migration of the giant planets was our stable Solar System, with Jupiter redirecting ice-rich small

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bodies inwards as one potential pathway to deliver water to the terrestrial planets and to allow life to thrive on Earth 40 (K. E. Mandt et al. 2024). The putative ejected giant planet fared the opposite fate, and was consigned to wander 41 the Solar neighborhood without a host star as a "rogue planet." Whether similar histories of dynamical interaction, 42 planet scattering, and ejection are common across planetary systems remains an open question due to the difficulty 43 of precisely mapping exoplanet system architectures and constraining the occurrence rate of isolated rogue planets 44 (T. Sumi et al. 2023). In this paper, we describe the orbital architecture of a nearby exoplanetary system whose 45 dynamically rich history has produced an architecture radically different from our Solar System's, with two giant 46 planets on misaligned, eccentric orbits, potentially as a result of a planetary ejection. The study of such an extreme 47 planetary system is enabled by our JWST (J. Rigby et al. 2023) detection of the potentially coldest and oldest planet 48 vet imaged. 49

14 Herculis is a nearby $(d = 17.898 \pm 0.009 \,\mathrm{pc}; Gaia \,\mathrm{Collaboration \ et \ al. 2021})$, metal-rich ([Fe/H] = $0.43 \pm 0.07; \mathrm{C}$. 50 Soubiran et al. 2010), K0-type, solar mass star hosting two giant planets (D. C. Bardalez Gagliuffi et al. 2021). These 51 two massive planets cause a reflex motion on the star detectable as a periodic change in its radial velocity and proper 52 motion. Radial velocity monitoring spanning over 20 years revealed a recurrent 5-year period due to the inner planet, 53 14 Her b, and a long-term trend (R. A. Wittenmyer et al. 2007) later confirmed as the widely-separated exoplanet 54 14 Her c by incorporating absolute astrometry from the Hipparcos and Gaia missions (D. C. Bardalez Gagliuffi et al. 55 2021). This analysis showed that the two planets in the system are roughly located at the equivalent semi-major axes 56 of the asteroid belt and Neptune's orbits in our own Solar System ($a_b = 2.845^{+0.039}_{-0.03}$ au, $a_c = 27.4^{+7.9}_{-16}$ au), yet on very 57 eccentric $(e_b = 0.369 \pm 0.003, e_c = 0.64 \pm 0.13)$, extremely misaligned orbits $(\Theta_{bc} = 96.3^{+36.8}_{-29.1})$. Only a handful of 58 other multi-planet systems have a measured orbital misalignment between two of their planetary orbits (e.g., π Men, 59 R. J. De Rosa et al. 2020; J. W. Xuan & M. C. Wyatt 2020; v And, B. E. McArthur et al. 2010; R. Deitrick et al. 2015; 60 Kepler-108, S. M. Mills & D. C. Fabrycky 2017; HAT-P-11, J. W. Xuan & M. C. Wyatt 2020; Q. An et al. 2025; T. 61 Lu et al. 2025; HD 73344, J. Zhang et al. 2024; HD 3167, V. Bourrier et al. 2021), yet none of these planets have been 62 directly imaged. While direct imaging is a challenging technique due to the large contrast between star and planet, it 63 can provide firsthand information on the planet, its exact location, and its atmosphere. 64

The measured dynamical masses of the 14 Her planets $(M_b = 9.1 \pm 1.9 M_J, M_c = 6.9^{+1.6}_{-1.0} M_J)$ at the age of the system 65 $(4.6^{+3.8}_{-1.3} \text{ Gyr})$ imply they have extremely cold temperatures (250 - 300 K; D. C. Bardalez Gagliuffi et al. 2021), making 66 them far more comparable to our own Jupiter (125 K; R. Hanel et al. 1981) than the majority of directly imaged 67 exoplanets (700-1700 K; B. P. Bowler 2016), except for ϵ Indi Bb (E. C. Matthews et al. 2024a), and TWA-7b (A. M. 68 Lagrange et al. 2025a). Cold exoplanets (< 500 K) emit most of their light in the mid-infrared, and are therefore 69 difficult to image from the ground in the optical or near-infrared, because of their intrinsic faintness and large flux 70 ratio, or 'contrast,' with their host stars. With its space-based, mid-infrared capabilities, JWST has the unique ability 71 to directly image much colder planets than have been studied before. 72

In this paper we present the first direct image of the nearby, cold, mature, giant planet 14 Her c with JWST/NIRCam 73 coronagraphy and revise its orbital parameters. This is the first direct image of a planet in a significantly misaligned 74 planetary system. In Section 2 we describe the new direct imaging observations with JWST/NIRCam and the process 75 to measure the photometry and astrometry of 14 Her c. In Section 3 we describe the updated orbit fitting, evolutionary 76 and atmospheric modeling, and dynamical simulations of the orbits. In Section 4, we discuss our results and their 77 implications for the mutual inclination of the planetary orbits, the likelihood of disequilibrium chemistry in the planet's 78 atmosphere, and the time evolution of the planetary orbits. We present our conclusions in Section 5. Technical details 79 about our methods on image reduction, orbit fitting, evolutionary and atmospheric modeling, and N-body simulations 80 are summarized in the Appendix (Sections A-C). 81

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2. OBSERVATIONS AND DATA REDUCTION

We used JWST/NIRCam (M. J. Rieke et al. 2023) to image 14 Her c as the main science objective of Cycle 2 program GO 3337 (PI: Bardalez Gagliuffi, Co-PI: Balmer). Our observing strategy relied on both Angular Differential Imaging (ADI) and Reference Differential Imaging (RDI) to perform starlight subtraction (K. B. Follette 2023, for a recent review). For validation, we used the pyNRC¹ (J. Leisenring et al. 2022) and PanCAKE² Python packages to determine optimal instrument readout patterns and estimate the contrast performance of the observations. Our

¹ https://pynrc.readthedocs.io/en/latest/

 $^{^2}$ https://aarynncarter.github.io/PanCAKE

14 Her C JWST/NIRCAM

NIRCam observations of 14 Her c were carried out between May 18, 2024 18:31:45 and May 19, 2024 01:08:45 (UTC) for a total of 7.8 hours (including observatory overheads) simultaneously with the F200W and F444W filters and using the MASKA335R coronagraph (J. E. Krist et al. 2010) at position angles 191.87° and 181.87°. This science observation used the SHALLOW4 readout pattern at 10 groups per integration and 96 integrations per exposure. Immediately following the observation of the target, we observed the reference star HD 144002 using the SHALLOW4 readout pattern, 8 groups per integration, and 16 integrations per exposure, with the 9-POINT-CIRCLE small grid dither pattern in an uninterruptable sequence to preserve the similarity of the telescope wavefront between observations. Observing the reference star with the small grid dither increases the diversity of the reference Point Spread Function (PSF) library (R. Soummer et al. 2014). We selected this reference star based on its relative on-sky proximity to 14 Her (ρ =3.67° in J2016), its brighter K-band magnitude, yet similar spectral type, and its low *Gaia* Renormalised Unit Weight Error

The observations were designed to detect a 250 K source at 1."3 from the star at a contrast of 10^{-6} with a 5 σ confidence in the F444W filter, while simultaneously collecting parallel images in the F200W filter where the planet signal was not expected. The limit in F200W-F444W color allows for the rejection of the vast majority of potential background contaminants, including stars, galaxies, and quasars, which would be at least as bright in F200W in comparison to F444W. The MASKA335R mask was chosen to balance inner working angle (IWA), raw starlight suppression performance, and reliable target acquisition.

(RUWE = 0.986, L. Lindegreen 2018), which indicates that it is likely a single star.

Image reduction and calibration followed previous work on the JWST/NIRCam coronagraph (A. L. Carter et al. 2023; K. Franson et al. 2024a; W. O. Balmer et al. 2025), the details of which are recorded in Appendix A³. The residual starlight in the coronagraphic images was modeled and removed using the Karhunen–Loève Image Projection (KLIP) algorithm (R. Soummer et al. 2012) through the Python implementation pyKLIP⁴ (J. J. Wang et al. 2015) wrapped by spaceKLIP⁵.

The JWST image of 14 Her c is shown in Figure 1. We detected a point source in the F444W filter with a signal-tonoise ratio of 5.7σ , an angular separation of 1.115 ± 0.005 at a position angle of $225.84^{\circ} \pm 0.26^{\circ}$ East of North, and apparent magnitude of 19.68 ± 0.07 mag with reference to Vega. There is also a spatially resolved background galaxy 1.15° away and to the SE of the star in both F200W and F444W images, whereas the point source only appears in the F444W image as expected for a cold giant planet. The location of our point source is consistent within 1σ with the latest predictions of the location of 14 Her c based on orbital solutions from the literature (G. F. Benedict et al. 2023, reproduced from their Table 10).

2.1. Contrast curves

We estimated the contrast performance of our observations using the spaceKLIP package following previous work (J. 119 Kammerer et al. 2022; A. L. Carter et al. 2023). We measured the annular standard deviation of the starlight-subtracted 120 images, masking the positions of the two sources within 2".0 (the planetary point source and the bright extended galaxy). 121 The raw contrast was corrected for small number statistics in the innermost annuli using the Student t-distribution 122 correction following D. Mawet et al. (2014). The corrected contrast was then calibrated into physical units using a 123 synthetic BT-NextGen model stellar spectrum (F. Allard et al. 2011) with parameters T_{eff} =5300 K, log(g)=4.5, and 124 [Fe/H]=+0.5 (G. Gonzalez et al. 1999; D. C. Bardalez Gagliuffi et al. 2021), scaled to match the Hipparcos/Tycho2 (E. 125 Høg et al. 2000), Gaia (Gaia Collaboration et al. 2022), and 2MASS (M. F. Skrutskie et al. 2006) photometry reported 126 for 14 Her. The coronagraph transmission function⁶ was applied to the calibrated contrast. Finally, we determined 127 the starlight subtraction throughput via injection-recovery tests⁷. Figure 6 shows our final calibrated contrast curves. 128 The observations are sensitive to sources with contrast $\sim 4 \times 10^{-7}$ at 1.0 in the F444W filter, and $\sim 3 \times 10^{-7}$ at 1.0 in 129 the F200W filter at 5 σ confidence, slightly exceeding our anticipated contrast performance of 10⁻⁶ at 1".0. 130

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2.2. Photometry and astrometry of 14 Her c

The process of the starlight subtraction with ADI and RDI oversubtracts astrophysical sources present in the image. We forward-modeled this degradation of the PSF (L. Pueyo 2016) in order to obtain accurate and unbiased astrometry and photometry of 14 Her c using pyklip (J. J. Wang et al. 2015; J. Golomb et al. 2021) and spaceKLIP

³ A notebook that can be used to reproduce the data reduction and image analysis described in Appendix A can be found online at the DOI: https://doi.org/10.5281/zenodo.15483953 (W. O. Balmer 2025)

⁴ https://pyklip.readthedocs.io/en/latest/

⁵ https://spaceklip.readthedocs.io/en/latest/

⁶ The NIRCam MASKA335R coronagraph transmission is an axisymmetric function of separation from the center of the mask, see Figure 4 in J. E. Krist et al. (2010).

⁷ We refer the reader to §3.1 and §3.2 in A. L. Carter et al. (2023) for additional details.



Figure 1. First direct image of 14 Her c. JWST/NIRCam coronagraphic imaging of the 14 Her system with the MASKA335R coronagraph (transmission indicated by gray shaded circles). North is up, east is left. Left: Prediction for the location of 14 Her c from a reproduction of the orbits presented in (G. F. Benedict et al. 2023), at the epoch of observation (MJD=60449), and the location of the point source detected in the F444W filter. Middle: A starlight-subtracted image taken with the F200W filter (1.755–2.227 μ m), showing extended emission from a background galaxy at about 1".5 to the SE from the host star. No other statistically significant point sources are apparent, as intended, given the cold temperature of the planet 14 Her c. Right: A starlight-subtracted image taken with the F444W filter (3.881–4.982 μ m), showing extended emission from the same background galaxy, and a point source at 1".1 to the SW with a contrast of 1 × 10⁻⁶. The location of the point source, detected with a contrast of 9.6 × 10⁻⁷, agrees within 1 σ with the predicted location for the planet, so we conclude we have detected 14 Her c.

(J. Kammerer et al. 2022; A. L. Carter et al. 2023; J. Kammerer et al. 2024; K. Franson et al. 2024b). Briefly, 135 an off-axis coronagraphic PSF model was generated using webbpsf at the approximate position of the candidate. 136 The model was scaled, translated, and subtracted from the data to compute a likelihood function, while the scale 137 and translation parameters were sampled iteratively using the MultiNest (via pyMultiNest) sampling algorithm (F. 138 Feroz et al. 2009; J. Buchner et al. 2014) with 400 live points. We accounted for the presence of correlated noise in 139 the image by sampling the length-scale of a Gaussian process, parameterized using a Matérn $\nu = 3/2$ kernel, which 140 approximates residual speckle noise (J. J. Wang et al. 2016). Once the astrometry and photometry were measured in 141 detector units, they were transformed into physical units accounting for the coronagraphic transmission, filter zero-142 points, and system distance (A. L. Carter et al. 2023; K. Franson et al. 2024b), with systematic uncertainties on 143 the star-behind-mask position (0.05 pix) and stellar magnitude (0.02 mag) added in quadrature (J. H. Girard et al. 144 2024). The point source has a relative RA, Dec. -0.800 ± 0.004 , -0.777 ± 0.006 (i.e., separation $\alpha = 1.115 \pm 0.005$ 145 and position angle PA = $225.84 \pm 0.26^{\circ}$, with a correlation $\rho = -0.5$). We derived an apparent magnitude of 146 19.68 ± 0.07 mag in the F444W filter, and an upper limit of 19.0 mag in the F200W filter. The corresponding fluxes in 147 SI units are $f_{\rm F444W} = 3.92 \times 10^{-19} \pm 2.5 \times 10^{-20} \,\mathrm{W/m^2/\mu m}$ and $f_{\rm F200W} = 7.25 \times 10^{-19} \,\mathrm{W/m^2/\mu m}$, respectively. These 148 fluxes correspond to absolute magnitudes of $M_{\rm F444W} = 18.42 \pm 0.07$ mag and $M_{\rm F200W} \ge 17.74$ mag. The candidate point 149 source was recovered in the F444W filter at a signal-to-noise ratio of SNR=5.7 σ , or a Bayesian evidence ratio of 150 $\ln(B_{10}) = \ln(Z_1/Z_0) = 115$ by comparing companion contrast to the annular contrast. 151

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2.3. Planetary Prior Probability Compared Against Interloper Probability

JWST is sensitive to background extragalactic sources far fainter than exoplanets in the Solar neighborhood. Previous high contrast imaging campaigns have ruled out sources surrounding 14 Her down to $15 - 30 M_J$ at 1".0 (K. L. Luhman & R. Jayawardhana 2002; J. Patience et al. 2002; J. C. Carson et al. 2009; T. J. Rodigas et al. 2011; S. Durkan et al. 2016). The red F200W-F444W color lower limit of the point source can be used to reject the vast majority of galactic contaminants. Since the probability of late T- or early Y-dwarf contaminants in such a compact field of view is vanishingly small (J. D. Kirkpatrick et al. 2024; E. Bogat et al. 2025), we conclude that the dominant source of contamination in our images is extragalactic sources.

In order to empirically estimate the number of contaminating sources that could confound a detection of 14 Her c, we calculated a space density of galaxies at all redshifts from JWST images that have similar observed characteristics as the planet. Following E. Bogat et al. (2025), we acquired the JADES GOODS-S Deep High Level Science Product v2 from MAST⁸ (D. J. Eisenstein et al. 2023; M. J. Rieke et al. 2023) covering 25 square arcminutes.

We define a contaminant as a JADES source that appears point-like in the F444W filter, with a magnitude within the 164 range of uncertainties of our candidate point source photometry, and with the F200W - F444W color lower limit of our 165 point source. Specifically, we selected galaxies with AB magnitudes and colors comprised between $[F444W_{AB mag}] =$ 166 22.9 ± 1.4 mag, and $[F200W_{AB mag} - F444W_{AB mag}] = 1.3$, and with a circular-equivalent size of FWHM < 4 pix. We 167 scaled the resulting number of sources by the sky area covered by the JADES GOODS-S Deep field to calculate the 168 space density of galaxies with these characteristics. As our candidate source has an F444W magnitude well within 169 the completeness limits of extragalactic surveys with JWST⁹, and since the completeness corrected source counts 170 for extragalactic surveys with JWST appear to agree well (E. Merlin et al. 2024, their Figure 7), we do not expect 171 any slight variation between JADES and other JWST deep fields to affect the robustness of the contaminant fraction 172 estimate presented here. 173

For the predicted location of 14 Her c (G. F. Benedict et al. 2023) and its 1, 2, and 3 σ contours (see leftmost panel of Figure 1), we expect on average 0.003, 0.013, or 0.052 contaminating galaxies, respectively. Within 2".0 of 14 Her A (see center and rightmost panel of Figure 1), we expect on average 0.2 contaminating galaxies. Therefore, given the small area where the planet is expected, the existence of an extragalactic source with photometric properties that mimic those of the planet is extremely unlikely. A larger number of extended and blue JADES sources are expected within 2".0, as evidenced by our detection of a resolved, blue galaxy to the SE of 14 Her A.

Balancing the extremely low likelihood that the point source is an extragalactic contaminant, and given that it is found in the predicted location, and with the expected luminosity for a giant planet of the age of the system (\sim 18 mag, see §3.2), based on evolutionary models (M. S. Marley et al. 2021a), we conclude that the observed point source to the SW of the star is indeed 14 Her c.

This background contaminant analysis emphasizes the importance of prior information, especially system-specific dynamical priors, when attempting to confirm the existence of directly imaged companions in the infrared with a facility as sensitive as JWST (E. Bogat et al. 2025). The strong prior prediction for the location of the planet allows us to robustly claim a reliable detection despite the 0.2 probability of finding a "14 Her c"-like source within the inner 2″.0 of our image, and without requiring a follow-up observation to confirm orbital and/or common proper motion of the point source.

Limits at longer wavelengths (with MIRI or ALMA) are invaluable for reducing the probability a candidate point 190 source is a background contaminant. For single epoch observations, including both NIRCam and MIRI coronagraphic 191 imaging appears to be the best practice (and, for nearby stars, may result in sensitivity to colder planets, see R. 192 Bowens-Rubin et al. 2025). For example, In A. M. Lagrange et al. (2025b), the flux limit of a contaminating galaxy 193 in the filter of interest (11.4 μ m) was 50% across their ~ 10" wide field of view. Only with deep upper limits from 194 archival SPHERE (and especially) ALMA observations, were they able to reduce the contaminant probability in the 195 1",5 immediately surrounding TWA 7 to 0.35%. Similarly, a second epoch was required for the eventual confirmation of 196 ε Indi Ab (E. C. Matthews et al. 2024b), where a low-significance early recovery of the candidate source in ground-197 based data was used to confirm the candidate's planetary nature. Strong dynamical priors, like those used to confirm 198 TWA 7b (A. M. Lagrange et al. 2025b) or 14 Her c, still contain a small probability of yielding false positives, but 199 they allow for greater confidence in the initial characterization of expected planets. Future long wavelength imaging 200 of 14 Her c with JWST would provide crucial color and temperature characterization, as well as incontrovertible 201 confirmation of the planet's detection. 202

The spatial scales where JWST reaches its deepest contrasts are necessarily those where the risk of background contamination becomes large. Future studies, especially large coronagraphic surveys of young moving group stars with NIRCam dual-band coronagraphy (GO 4050, 5835, 6005, 7651) will need to rely heavily on ground-based upper limits

⁸ https://doi.org/10.17909/8tdj-8n28

⁹ JADES, and other JWST surveys, are 100% complete to at least $[F444W_{AB mag}] = 28 \text{ mag}$, whereas our point source has $[F444W_{AB mag}] = 22.9 \pm 1.4 \text{ mag}$. See Figure 4 of E. Merlin et al. (2024) for more details.

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from the literature, as well as any and all available dynamical limits to confirm cold planets that can currently only be detected with JWST.

3. ANALYSIS AND RESULTS 3.1. Orbit fitting



Figure 2. Sky projection of the architecture of the 14 Her system. The visual orbits for both planets, colored according to the time after the reference epoch 2020.0, MJD=58849.0. The new NIRCam relative astrometry of 14 Her c strongly constrains the relative orientation of the two planets' possible orbital planes.

We use our new JWST relative astrometry of 14 Her c to update the orbital parameters of the system, combining this data set with literature RVs from the ELODIE (D. Naef et al. 2004), HIRES (L. J. Rosenthal et al. 2021), HRS (G. F. Benedict et al. 2023), and APF (S. S. Vogt et al. 2014) instruments spanning 25 years and absolute astrometry from Hipparcos and Gaia (T. D. Brandt 2018). We fit a total of 21 parameters with our 571 data points (3 from Gaia-Hipparcos absolute astrometry, 567 RV points, and 1 relative astrometry measurement from JWST) using two ²¹⁵ publicly-available orbit fitting codes: orvara¹⁰ (T. D. Brandt et al. 2021) and orbitize!¹¹ (S. Blunt et al. 2020). ²¹⁶ Both of these orbit fitters use Bayesian inference with a Markov Chain Monte Carlo (MCMC) sampler to iteratively ²¹⁷ fit the data to Keplerian orbit models. Specifically, they use a Python implementation of a parallel-tempered version ²¹⁸ of the emcee (D. Foreman-Mackey et al. 2013) MCMC algorithm, namely ptemcee (W. Vousden et al. 2021). These ²¹⁹ two codes differ in their implementation of implicit priors, their treatment of parallaxes, their flexibility incorporating ²²⁰ arbitrary absolute astrometry, and their computational speed.

Multi-planet systems are fit by iteratively solving two-body problems starting with the outermost companion. We used a Gaussian prior on the parallax of the star (π =55.866 ± 0.029; (Gaia Collaboration et al. 2022)), a log-flat prior on the primary mass and RV jitters (one per instrument), uninformative priors on projections of the eccentricity, mean longitude, and ascending node, and a sin *i* prior on orbital inclination to give equal probability to all possible orbital orientations.

Our results with both orbit fitters use the same priors and data sets, and statistically agree on the accuracy and precision of the posterior probability distributions despite starting with different initial conditions and running for a different number of total steps, an indication that our results are robust and have converged. In Table 1, we present the results from the longest run starting with agnostic initial conditions with orbitize!. Details on the initial conditions and code setup for each orbit fitter can be found in the Appendix B.

Our measured relative astrometry of 14 Her c establishes the tangential direction of the reflex motion that the planet 231 exerts on its host star, helping to apportion the contribution of each planet to the total acceleration of 14 Her between 232 the Hipparcos and Gaia measurements. The visual orbits for the two planets are shown in Figure 2, and model fits 233 to the stellar radial velocities are shown in Figure 8. Table 1 records a summary of orbital parameter values. The 234 new orbital solution for planet c gives a mass of $M_c = 7.9^{+1.6}_{-1.2} M_J$, a semi-major axis of $a_c = 20.0^{+12.0}_{-4.9}$ au, and an eccentricity of $e_c = 0.52^{+0.16}_{-0.12}$, consistent with previous results (D. C. Bardalez Gagliuffi et al. 2021; F. Feng et al. 235 236 2022; G. F. Benedict et al. 2023). Two families of supplementary solutions for the inclination of 14 Her b arise from our orbit analysis: $i_b = 32.70^{+7.45}_{-4.01} \circ$ and $i_b = 146.90^{+4.58}_{-9.74} \circ$ driven by our lack of knowledge of the longitude of the 237 238 ascending node for the inner planet (Ω_b) , which dictates the direction of a planet's motion along its orbit (as noted 239 by F. Feng et al. 2024, for the case of 14 Her, either solution can be missed due to insufficient posterior sampling). 240 Inclusion of HST/FGS observations (G. F. Benedict et al. 2023), and follow-up JWST astrometry of 14 Her c and/or 241 future direct imaging of 14 Her b with the Nancy Grace Roman Space Telescope (T. D. Groff et al. 2021), will provide 242 crucial additional constraints on the relative orientations of the orbits, helping to further resolve the architecture of 243 the system. 244

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3.2. Evolutionary and atmospheric modeling

Using our estimated dynamical mass for 14 Her c and the age posterior from the stellar characterization presented in 246 (D. C. Bardalez Gagliuffi et al. 2021), we calculated fundamental parameters for the c planet with the Sonora-Bobcat 247 cloudless substellar evolutionary models (M. S. Marlev et al. 2021b), assuming a metallicity of [Fe/H]=+0.5, representa-248 tive of the stellar metallicity (G. Gonzalez et al. 1999; R. E. Luck & U. Heiter 2006). We linearly interpolated across the 249 publicly available model grid and predict $T_{\rm eff}=300\pm30\,\mathrm{K}$, $\log(g)=4.25\pm0.15$, $R_{\rm pl}=1.03\pm0.01\,\mathrm{R}_{\rm j}$, $\log(L/L_{\odot})=-7.1\pm0.2$. 250 Integrating the NIRCam/F444W flux for a Sonora-Bobcat atmospheric model with these parameters, we predict an 251 apparent magnitude of 17.98 mag, which is 1.69 mag brighter than our observed apparent magnitude in F444W (see 252 Section 2). Simultaneously fitting the Sonora-Bobcat atmospheric models to our F444W photometry and F200W 253 limit, with T_{eff} as a free parameter and the other parameters fixed to their evolutionary values, we find $T_{\text{eff}}=210\,\text{K}$. 254 This $\sim 90 \,\mathrm{K}$ tension can be reasonably attributed to carbon disequilibrium chemistry driven by vertical mixing, the 255 presence of ice clouds, an enhanced metallicity (K. J. Zahnle & M. S. Marley 2014a; B. Lacy & A. Burrows 2023) 256 or some combination of these factors. Vertical mixing throughout the atmosphere can dredge up molecules that are 257 formed at warm temperatures in the lower atmosphere and mix them into the cold, upper atmosphere faster than 258 the chemical reaction timescale. This imbalance is most prominent among carbon and nitrogen molecules in objects 259 colder than 500 K (K. J. Zahnle & M. S. Marley 2014a; B. Lacy & A. Burrows 2023). Carbon disequilibrium chemistry 260 imparts deep CO and CO₂ absorption between $3-5\,\mu m$ (B. E. Miles et al. 2020; S. A. Beiler et al. 2023, 2024a) in 261 the spectra of substellar objects, even though the dominant carbon species at these temperatures should be CH_4 in 262 chemical equilibrium (B. Lacy & A. Burrows 2023; K. J. Zahnle & M. S. Marley 2014a). Clouds made of water ice 263

¹⁰ https://github.com/t-brandt/orvara

¹¹ https://orbitize.readthedocs.io/en/latest/



Figure 3. Carbon disequilibrium chemistry and water clouds are likely in 14 Her c's atmosphere. JWST/NIRCam photometry of 14 Her c (F444W flux as a black hexagon, F200W upper limit as a black triangle) compared to atmospheric model spectra (colored lines) integrated over the filter bandpasses (colored circles, squares, diamonds). Publicly available Sonora Bobcat (M. S. Marley et al. 2021a) and Sonora Elf Owl (S. Mukherjee et al. 2024b) models (in dark blue and green, respectively) are unable to reproduce the data with temperatures in agreement with evolutionary model predictions. Custom PICASO models with an updated treatment of carbon disequilibrium chemistry (light blue) brings the models in better alignment with the observations and evolutionary model predictions. Adding water ice clouds (red) to these custom atmospheric models brings the observations into agreement at 1 σ with both the atmospheric and evolutionary models.

particles can also absorb or scatter outbound light, and redistribute it to different wavelengths. To explore the effects of carbon disequilibrium chemistry and cloud formation on our measured F444W photometry, we generated a custom mini-grid of atmospheric models matching the metallicity of the star ([Fe/H] = +0.5), assuming a solar C/O, and including disequilibrium chemistry and water ice clouds based on the **Sonora Elf Owl** family of models (S. Mukherjee et al. 2024b). Details are described in Appendix C.

Figure 3 shows that our JWST photometry in F444W is consistent with a cloudy atmosphere with carbon disequilibrium chemistry driven by strong vertical mixing (B. E. Miles et al. 2020; S. A. Beiler et al. 2023, 2024a) at $T_{\rm eff}$ = 275 K and log g= 4.25. This result puts 14 Her c in the running for the coldest directly imaged exoplanet to date, a title currently held by Epsilon Indi Ab (E. C. Matthews et al. 2024a). Although these two planets have not yet both been imaged at equivalent wavelengths, the mid-infrared color of Epsilon Indi Ab similarly suggests a temperature of $T_{\rm eff}$ = 275 – 300 K.

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3.3. Dynamical simulations

We explored the present-day dynamical evolution of the system by performing secular (i.e. orbit-averaged) three-body simulations using the publicly available KozaiPy software¹². KozaiPy solves the equations of motion for three-body hierarchical systems ($a_b \ll a_c$) presented in P. P. Eggleton & L. Kiseleva-Eggleton (2001); D. Fabrycky & S. Tremaine

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(2007) to octupole order $(a_b/a_c)^3$ (S. Naoz et al. 2013). These packages include effects from equilibrium tides and 279 general relativity, but as both planets are relatively far from the host star, such short-range effects are not impactful. 280 In this limit, the semimajor axes of both planets remain fixed while mutual gravitational perturbations cause the 281 eccentricities and inclinations to oscillate. We note that this level of approximation is strictly valid only for an inner 282 test particle influenced by a massive, arbitrarily eccentric external perturber, and as such may not fully capture some 283 relevant dynamics in the 14 Her system due to its similarly massive planets. There is no existing analytic prescription 284 describing this regime, which is typically probed with direct N-body simulations (J. Teyssandier et al. 2013). We 285 reserve detailed exploration of this for future work. 286

We sampled ~ 10,000 parameter vectors from the posterior distribution derived from orbitize! and integrated them forward in time 10 Myr, tracking the evolution of the orbital elements of both planets using orbit-averaged simulations assuming a hierarchical approximation $(a_b \ll a_c)$. All orbital solutions show substantial eccentricity and inclination oscillations for both planets as a result of strong secular perturbations. Figure 5 shows the distribution of the eccentricity oscillation amplitude of 14 Her b $\Delta e_b \equiv \max e_b - \min e_b$, as well as examples of two representative simulations – one characterized by moderate eccentricity and inclination oscillations, and one by much stronger oscillations.

4. DISCUSSION

4.1. On the mutual inclination of the 14 Her planets

With our new orbital solutions, we revise the mutual inclination angle Θ between the two orbital planes, defined as

$\cos\Theta = \cos i_b \cos i_c + \sin i_b \sin i_c \cos \left(\Omega_b - \Omega_c\right)$

in e.g., D. C. Bardalez Gagliuffi et al. 2021; I. Czekala et al. 2019. This results in a bimodal posterior distribution of 296 mutual inclinations of $\Theta = 32^{+13.6}_{-15.1}$ and $\Theta = 145.0^{+15.8}_{-11.1}$, for i_b greater than or less than 90°, respectively. These 297 values represent roughly a factor of two improvement in precision compared to the previous estimate of the mutual 298 inclination before our relative astrometry measurement of 14 Her c with JWST ($\Theta = 96.3^{+36.8}_{-29.1}$, D. C. Bardalez 299 Gagliuffi et al. 2021). The nonzero mutual inclination between the orbits of 14 Her b and c and large eccentricities are 300 in stark contrast with the planets in our own Solar System, as well as younger, directly imaged multiplanet systems 301 like HR 8799 (C. Marois et al. 2008), β Pictoris (A. M. Lagrange et al. 2010), and HD 206893 (S. Hinkley et al. 2023) 302 that have multiple planets on (roughly) coplanar, low eccentricity orbits (B. P. Bowler et al. 2020). 303

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4.2. Potential for disequilibrium chemistry in the atmosphere of 14 Her c

³⁰⁵ 14 Her c is over a million times fainter than its host star at $4.4 \,\mu\text{m}$ (a contrast of $9.6 \pm 0.5 \times 10^{-7}$, see Figure 6), and ³⁰⁶ roughly one magnitude fainter than the coldest isolated brown dwarf known, WISE J0855-0714 (M. J. Rowland et al. ³⁰⁷ 2024) in the comparable Spitzer filter centered at $4.5 \,\mu\text{m}$. The 90 K degree tension between the temperatures from ³⁰⁸ evolutionary and spectral models is $> 3 \sigma$ significant, suggesting the presence of additional sources of $4.4 \,\mu\text{m}$ opacity ³⁰⁹ in the planet's atmosphere such as clouds or disequilibrium chemistry.

Our custom model fits imply that 14 Her c should have a deep CO_2 absorption feature at 4.2 μ m (S. A. Beiler et al. 310 2024b), which can be tested using follow-up JWST coronagraphic images with narrower bandwidth filters (W. O. 311 Balmer et al. 2025). Similarly, our photometry implies that other cold planets like 14 Her c are likely slightly fainter 312 at $4.4 \,\mu\mathrm{m}$ than expected for their mass and age. Future JWST observations of 14 Her c with multi-band photometry 313 across the near and mid-infrared could feasibly quantify the thermal emission, cloud opacity slope, and CO₂, CO, and 314 NH₃ absorption feature strengths predicted by these models. Direct spectroscopy with JWST may be able to further 315 refine the molecular abundances in the planet's atmosphere, although this will be challenging due to the planet's high 316 contrast. These observations would provide the first glimpses into the complexity of this field-age, giant exoplanet 317 atmosphere as a benchmark for other cold exoplanets and Y-type brown dwarfs, yielding new insights into the physics 318 and chemistry occurring in low temperature giant planet atmospheres. 319

4.3. A cold planet in a dynamically hot system

The unusual present configuration of this system is not representative of most observed multi-planet systems and instead points to past and ongoing dynamical interactions. The results from our dynamical simulations (see Section 3.3) indicate that both planets in the 14 Her system are currently experiencing significant secular eccentricity and inclination



Figure 4. The posterior distribution of mutual inclination angles Θ between the orbits of 14 Her b and c, compared to the Sine prior. The constraint on the mutual inclination is driven by the likelihood function and not the prior.

oscillations. While it is impossible to directly compare the magnitude of these excursions to the exoplanet population at large (as such comprehensive detailed dynamical modeling does not exist for all systems), an illustrative comparison can be made with the Solar System. The largest amplitude eccentricity excursions experienced by a Solar System planet are of order ~ 0.1 by Mercury, whereas 14 Her b, on average, experiences oscillations with nearly five times this amplitude. This behavior makes 14 Her the only currently known dynamically "hot" multi-planet system with an imaged planet¹³. However, even though the orbital parameters vary periodically, the system is stable on this timescale. Planet-planet scattering, including a planetary ejection, was proposed as a potential hypothesis to explain the origin

Planet-planet scattering, including a planetary ejection, was proposed as a potential hypothesis to explain the origin of this peculiar system architecture (D. C. Bardalez Gagliuffi et al. 2021). With our new orbital constraints, future N-body simulations exploring this and other initial scenarios will be key to gauge the feasibility of this mechanism in shaping the configuration of this system and its relative occurrence among the long-period exoplanet population. Ejections of giant planets may then be a common avenue to produce the observed population of "rogue" planets in our galaxy (T. Sumi et al. 2023).

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5. CONCLUSIONS

³³⁷ In this letter we present the first direct images of 14 Her c. The key takeaways of our study are as follows:

1. Coronagraphic imaging of 14 Her with JWST/NIRCam achieved deep contrasts ($< 10^{-6}$) at thermal wavelengths (4.5 µm) and spatial scales between 15-150 au. These observations detected the known planet 14 Her c at $> 5 \sigma$ confidence.

¹³ For example, the dynamically "cold" directly imaged multi-planet system β Pictoris bc likely experiences secular eccentricity oscillations of order $\Delta e < 0.2$ (S. Lacour et al. 2021), and the HR 8799 bcde system likely experiences oscillations of order $\Delta e < 0.05$ (J. J. Wang et al. 2018).



Figure 5. Example dynamical simulations, initialized from different parameter vectors from the orbitize! posterior distribution. The left and right columns show examples of lower and higher amplitudes of secular oscillations, as seen in the eccentricity variations of both planets and the mutual inclination variations. The histogram in the bottom panel shows the distribution of Δe_b across all simulations, and the values corresponding to the two example simulations are shown with the vertical red lines.

- 2. The planet appears within 1σ of its predicted location from orbits fit to previous absolute astrometry and radial velocity measurements. The probability of a chance alignment with a background source are negligible compared to the likelihood the source is 14 Her c.
- 3. 14 Her c ($T_{\text{eff}} \sim 275 300 \text{ K}$) rivals ϵ Indi Ab ($\sim 275 300 \text{ K}$, E. C. Matthews et al. 2024b) and TWA 7 b ($\sim 315 \text{ K}$, A. M. Lagrange et al. 2025b) as one of the coldest planets yet directly imaged, and with ϵ Indi Ab ($\sim 3.5 \text{ Gyr}$, E. C. Matthews et al. 2024b) as one of the oldest ($\sim 4.6 \text{ Gyr}$).
- 4. Temperature estimates for 14 Her c disagree slightly within 90 K or 1σ between the estimate from dynamical mass and age and that from the F444W photometry. This tension between estimates could be explained by

the presence of carbon disequilibrium chemistry and/or water ice clouds in the atmosphere. See Figure 3 for atmospheric modeling.

5. The misalignment between orbits identified in D. C. Bardalez Gagliuffi et al. (2021) remains. With our new detection, we have refined the parameters of both planetary orbits in the system and constrained the misalignment more precisely. Only five other multi-planet systems with measured orbits exhibit a significant misalignment, and so far 14 Her is the only one with a directly imaged planet.

6. The unusual system architecture of 14 Her c is suggestive of dramatic past and present dynamical interactions. Our preliminary dynamical simulations indicate ongoing secular eccentricity and inclination oscillations with large eccentricity excursions roughly 5 times those of Mercury.

This system is a unique benchmark to describe the dynamical evolution of multi-planet systems and the atmospheric properties of Jupiter analogs. Future multi-band imaging or cross correlation spectroscopy with JWST can provide a glimpse into the spectral energy distribution and the atmospheric composition of this planet. 14 Her is an exciting target for the Coronagraphic Instrument aboard the Roman Space Telescope. Precisely constraining the location of the inner planet will establish both planetary orbits in the system, the degree of orbital misalignment, and exclude a subpopulation of orbital solutions to improve our knowledge on the ongoing dynamical interactions of the system.

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AUTHOR CONTRIBUTIONS

D.B.G. and W.O.B. planned and proposed the James Webb Space Telescope observations, led the collaboration, and wrote the manuscript. W.O.B. and L.P. led the JWST image processing, starlight subtraction, photometric and astrometric measurements. D.B.G., W.O.B., M.G., and T.D.B. led the orbit fitting with both orvara and orbitize!. D.B.G., W.O.B. estimated fundamental parameters with evolutionary models. S.M., T.L., M.R., B.B. designed and ran secular dynamical simulations.J.M., C.M., B.L. developed a mini-grid of atmospheric models and fit the measured JWST photometry to them. J.G. advised on observation planning for the NIRCam coronagraph. E.C.M., A.C., B.P.B., J.F., C.F., E.R. provided comments and expertise throughout the analysis.

Facilities: JWST(NIRCam), OHP:1.93m(ELODIE), Keck:I(HIRES), Smith(Cross-Dispersed Echelle Spectrograph), APF, HIPPARCOS, Gaia

³⁸³ Software: astropy, pyKLIP, spaceKLIP, orbitize!, orvara, KozaiPY, PICASO

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APPENDIX

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A. IMAGE REDUCTION

The uncalibrated Stage 0 (*uncal.fits) data products were acquired from the Barbara A. Mikulski Archive for Space Telescopes (MAST) ¹⁴ and processed with spaceKLIP¹⁵, a community developed pipeline for high contrast imaging

 14 The data described here may be obtained from the MAST archive at doi:10.17909/gx61-s247

¹⁵ https://spaceklip.readthedocs.io/en/latest/

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with JWST (J. Kammerer et al. 2022). spaceKLIP wraps the jwst pipeline (H. Bushouse et al. 2023) for basic 388 data processing steps with modifications for coronagraphic imaging reduction. Data reduction via spaceKLIP for 389 observations using the F444W filter and MASK335R coronagraph has been described at length (J. Kammerer et al. 390 2022; A. L. Carter et al. 2023; K. Franson et al. 2024b; J. Kammerer et al. 2024; W. O. Balmer et al. 2025). We 391 used spaceKLIP v2.1, via github commit #11df3a1, and jwst v1.18; the calibration files were from CRDS v12.1.5 392 and the jwst_1364.pmap CRDS context¹⁶. Briefly, the data were fit "up the ramp" using the "Likely" algorithm 393 described in (T. D. Brandt 2024a,b) and transformed from Stage 0 images into Stage 2 (*calints.fits) images, using a 394 jump threshold of 4 and 4 pseudo-reference pixels on all sides of the subarrays; this process collates the frames (non-395 destructive reads and averages of the detector) into integrations, which end with destructive readouts of the detector, 396 while using the differences between groups to correct for cosmic rays and other artifacts. The 1/f noise typical of 397 thermal imaging with HgCdTe arrays was mitigated using a median filter computed along each column. We skipped 398 dark current subtraction following (A. L. Carter et al. 2023). Pixels flagged by the jwst pipeline as well as 5σ outliers 399 detected post facto using sigma clipping were replaced with a 2-dimensional interpolation based on a 9-pixel kernel. 400 We also identified additional pixels affected by cosmic rays by flagging pixels with significant temporal flux variations 401 across integrations and replaced them by their temporal median. Subsequently, the images were blurred above the 402 Nyquist sampling criterion, using a Gaussian with a FWHM of 2.70 for the F444W/LW detector and 2.77 for the 403 F200W/SW detector. These values ensure that sharp features in the data do not create artifacts when Fourier shifts 404 are applied to the undersampled images. The position of the star behind the coronagraph was estimated by fitting 405 a model coronagraphic PSF from webbpsf_ext¹⁷ to the first science integration. All subsequent images were shifted 406 by this initial offset. Images were cross-correlated to the first science integration, and these small shifts were applied 407 to each integration to center the entire observing sequence to the first science integration. The recovered shifts were 408 equivalent to and reproduced the small grid dither sequence that was commanded. 409

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A.1. Starlight subtraction and contrast estimation

The residual starlight in the coronagraphic images was modeled and removed using the Karhunen–Loève Image 411 Projection (KLIP) algorithm (R. Soummer et al. 2012) through the Python implementation pyKLIP¹⁸ (J. J. Wang 412 et al. 2015) wrapped by spaceKLIP. This algorithm uses Principal Component Analysis (PCA) to create an orthogonal 413 basis set of eigenimages from the reference images. The science images are projected onto this basis to isolate and 414 remove the contribution from the stellar PSF common between the reference and science images. This can be done 415 on annular or radial subsections of the data by specifying a number of **annuli** and **subsections** in which to split the 416 data, while the number of eigenimages used to construct the PSF model are specified with the numbasis parameter 417 (sometimes referred to as the number of "KL modes"). 418

We used ADI and RDI to create our model PSF and subtracted the starlight with annulus=1, subsections=1, 419 and $numbasis \in [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 25, 50, 100]$. In the F200W filter, an extended source (a background galaxy) is 420 visible in all KL modes at a separation of 1.5 to the SE, and becomes very apparent by the 6^{th} KL mode. In the F444W 421 filter, this same galaxy appears by the 5^{th} KL mode subtraction, and another source, a point source, becomes apparent 422 to the SW. By the 10^{th} KL mode, most other speckles in the image have been suppressed, leaving the galaxy at 1".5 to 423 the SE in both filters, a few faint, extended sources beyond 2".0 (one at 4".0 to the NE, and one at 8".9 to the N), and 424 the point source to the SW in F444W. We detected no other point sources in either filter. We verified that the point 425 source appears in both roll angles and rotates with the astrophysical scene, not the detector frame. The signal-to-noise 426 ratio of the source climbs from <1 to 5.7 between numbasis 1 and 5, and plateaus about this value for numbasis>5. 427 We tested the robustness of the source to the starlight subtraction by varying KLIP parameters, and found that the 428 point source persists for annuli $\in [2-16]$ and subsections $\in [2-8]$, numbasis >5. The significance of the source does 429 not vary dramatically with the choice of KLIP parameter, but is greatest for the simplest, least "aggressive" choice in 430 parameters, annuli=1, subsections=1 because there is the least self-subtraction for these parameters (J. I. Adams 431 Redai et al. 2023). We also verified that the source persists, albeit at lower SNR, in subsets of the science integrations; 432 we were able to detect the source at $\geq 4\sigma$ in up to a third of the total dataset, regardless of which frames were selected. 433 Since the contrast and position of the point source agrees well with the mass and position predicted for the epoch 434 of observation based on orbits for 14 Her c from (D. C. Bardalez Gagliuffi et al. 2021) and (G. F. Benedict et al. 435

 $^{^{16}\} https://jwst-crds.stsci.edu/display_context_history/$

 $^{^{17}}$ https://github.com/JarronL/webbpsf_ext

¹⁸ https://pyklip.readthedocs.io/en/latest/



Figure 6. Contrast curve for the NIRCam observations of 14 Her using the 335R coronagraph. The F444W and F200W 5 σ contrast curves are shown as solid and dashed lines respectively. The likely detection of 14 Her c at ~1."1 is plotted as an black circle and error bar. The nominal 335R inner working angle ("IWA"), where the coronagraph transmission reaches 50%, is indicated by a vertical dashed line. *Takeaway*: Our detection of 14 Her c is statistically significant.

⁴³⁶ 2023), we proceed to estimate its astrometry and photometry using the annuli=1, subsections=1, numbasis=25
 ⁴³⁷ PSF subtracted images (Figure 1).

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A.2. Forward model subtraction of both sources

The forward modeling of the point source, 14 Her c, is described in §2.1. In this section, we briefly describe a 439 simplistic forward model for the extended source, the background galaxy, in the F444W filter and present the residual 440 images for the forward modeling. The procedure for modeling the extended source follows from the point source 441 forward model, except that at each step the webbpsf model is convolved with a 2D Gaussian parameterized by a 442 FWHM in the x and y directions and a correlation term θ . This model does not fully capture the structure of the 443 source, as residuals are apparent to the SE of the central source, but serves to describe it at first order. Figure 7 444 illustrates the F444W image (Figure 1), the same image with the background galaxy subtracted, and with both sources 445 subtracted. 446

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B. ORBIT FITTING

B.1. orvara

For an initial orvara run, we used all three datasets with 100 walkers over 30 temperatures, 1 million steps per walker (i.e., 500,000 steps for each planet) and saved every 50^{th} step for inference, starting with the median parameter values from the posteriors published in (D. C. Bardalez Gagliuffi et al. 2021) as initial conditions. We constrained the RV jitter for each instrument to a $10^{-5} - 10 \text{ m/s}$ range. The total chain length per walker was 20,000 out of which the first 500 steps were discarded as burn-in.

The single epoch of JWST relative astrometry for the 14 Her c planet helped to strongly constrain its orbital parameters. However, our lack of constraint on the longitude of the ascending node for 14 Her b produced a bimodal distribution for its orbital inclination. About 2/3 of the orbit posteriors were consistent with an inclination of b lower than 90°, whereas the remaining 1/3 of orbits had inclinations for b greater than 90°. To explore this degeneracy, we ran new orbit fits to produce longer chains of 3 million steps per walker divided evenly over the two planets, using



Figure 7. Forward modeling of sources in the NIRCam F444W image. (a) Reproduction of the PSF subtracted image in Figure 1. The two prominent sources are an extended source (a galaxy) to the SE and a point source (14 Her c) to the SW. (b) The residuals after the subtraction of a simple forward model of the background galaxy, a webbpsf point source convolved by a 2D Gaussian. Small (10%) residuals to the SE of the center of the galaxy are apparent. The visual significance of 14 Her c is apparent, as the galaxy has been suppressed. (c) The residuals of the image after the point source forward model for 14 Her c has been subtracted.

⁴⁵⁹ 100 walkers over 30 temperatures. On separate runs, we tried each family of inclinations for b and the associated
⁴⁶⁰ parameters for b and c as initial conditions. The total chain length used for inference on each run had 60,000 steps
⁴⁶¹ with 3000 steps discarded as burn-in, both with a mean acceptance fraction of 0.029.

It appears as if the initial run with 1 million steps had not yet converged and based on the starting conditions, which initialized at an inclination of $32.7^{+3.2}_{-5.3}$ ° for b (D. C. Bardalez Gagliuffi et al. 2021), gave preference to this family of solutions while only starting to explore the family of supplementary inclinations greater than 90°. The subsequent longer runs reversed the proportion of orbits of 14 Her b with each inclination, with only 1/5 of posteriors consistent with a $i_b < 90^\circ$ regardless of the initial conditions of b inclinations (i.e., below or above 90°).

B.2. orbitize!

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We corroborated our results with an independent orbit fit using orbitize!. We set normally distributed priors on 468 the host star mass $(M_*=0.98\pm0.04; (D. C. Bardalez Gagliuffi et al. 2021))$ and the system parallax $(\pi=55.866\pm0.029;$ 469 Gaia Collaboration et al. 2022)). We adopted uniform priors between -5 and 5 km/s for the RV zero points, and log 470 uniform priors between 10^{-5} and 10^2 km/s for the RV jitter nuisance parameters. We restrict the semi-major axes for 471 the inner and outer planets not to cross, placing log-uniform priors between 0.1 and 5 au for the inner, and between 5 472 and 500 au for the outer. Similarly, we place log-uniform priors on the planet masses ranging from 0.2 to 20 Jupiter 473 masses. We adopted uninformative priors on the eccentricity and the angles describing the visual orbital elements for 474 the two planets (Table 1; (S. Blunt et al. 2020)). 475

For our orbitize! run we use 100 walkers (initialized randomly within the prior space) over 20 temperatures and 476 2.5×10^6 steps. We discarded the first 2.25×10^6 steps as burn-in and thinned the sampler by a factor of 10, saving only 477 every 10^{th} step, resulting in a final posterior distribution with 2.5×10^6 orbits, each composed of 26 parameters. The 478 fit yields two modes in the posterior distribution on i_b and Ω_b , due to a degeneracy in the visual orbit of the inner 479 planet b, while the mode of the parameters describing the orbit of c all have a tail of solutions that are correlated 480 with the RV jitter terms, due to the fractional phase coverage of the planet's orbit by each instrument. Even after 481 the exhaustive MCMC run, the two modes are not equivalently weighted, and the solutions with $i_b = 147^{+4.57}_{-9.68}$ 482 are more numerous, at a ratio of about 3 to 1, compared to the solutions with $i_b = 32.46^{+7.31}_{-4.25}$ °. This results in a posterior distribution of mutual inclinations of $\Theta = 32^{+13.6}_{-15.1}$ ° and $\Theta = 145.0^{+15.8}_{-11.1}$ °, for i_b greater than or less than 483 484 90° , respectively. We adopt this set of posterior parameters and present the median and 1 σ confidence intervals of the 485 marginalized posterior distribution in Table 1. Figure 8 visualizes the radial velocity measurements compared to 100 486 randomly drawn posterior models, and Figure 2 shows the sky-projected visual orbits for both planets on the same 487 scale. Figures 9 and 10 show the posterior distribution on the orbital elements for 14 Her b and c respectively, without 488 the nuisance parameters. 489



Figure 8. The stellar radial velocities driven by the orbits of both planets, as measured by various instruments. The $\sim 5 \text{ yr}$ modulation from 14 Her b is apparent, as is the long term variation due to 14 Her c, although there is not complete coverage of the outer planet's orbit.

1 1 1 1 1 1 1 1 1 1	14	Her	\mathbf{C}	J	WS	Γ/Γ	NIR	Сам
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Parameter	Description	Units	Prior	Max. A-posteriori	Median and 68% CI
$a_{ m b}$	Semi-major axis	au	Log-uniform [0.1, 5]	2.839	$2.839^{+0.039}_{-0.041}$
$e_{ m b}$	Eccentricity		Uniform $[0,1]$	0.3683	$0.3683^{+0.0029}_{-0.0029}$
$i_{ m b}$	Inclination	degree	Sine [0,180]	147.8	$146.7^{+4.584}_{-9.740}$
$i_{ m b}$ *	Inclination	degree	Sine [0,180]	29.79	$32.66_{-4.011}^{+7.448}$
$\Omega_{ m b}$	Longitude of the Ascending Node	degree	Uniform [0,360]	202.7	$197.8^{+4.240}_{-5.615}$
$\Omega_{ m b}$ *	Longitude of the Ascending Node	degree	Uniform [0,360]	44.12	$44.69^{+3.438}_{-4.011}$
$ au_b$	Relative Periastron \ddagger		Uniform $[0,1]$	0.7670	$0.7672^{+0.0013}_{-0.0013}$
$a_{ m c}$	Semi-major axis	au	Log-uniform $[5, 500]$	15.1	$20.0^{+12.0}_{-4.9}$
$e_{ m c}$	Eccentricity		Uniform $[0,1]$	0.40	$0.52^{+0.16}_{-0.12}$
$i_{ m c}$	Inclination	degree	Sine [0,180]	114.0	$116.3^{+24.64}_{-9.167}$
$\omega_{ m c}$	Argument of periastron †	degree	Uniform [0,360]	173.0	$172.5_{-4.584}^{+4.011}$
$\Omega_{ m c}$	Longitude of the Ascending Node	degree	Uniform [0,360]	206.8	$205.1^{+7.448}_{-10.31}$
$ au_c$	Relative Periastron \ddagger		Uniform $[0,1]$	0.66	$0.78^{+0.11}_{-0.12}$
π	Parallax	mas	$\mathcal{N}(55.866, 0.029)$	55.871	$55.866^{+0.028}_{-0.029}$
$\gamma_{ m APF}$	RV ZP	$\rm km/s$	Uniform	0.044	$0.031\substack{+0.013\\-0.017}$
$\sigma_{ m APF}$	RV jitter	$\rm km/s$	Log-uniform	0.00345	$0.00347^{+0.00027}_{-0.00023}$
γ_{ELODIE}	RV ZP	$\rm km/s$	Uniform	-0.028	$-0.041^{+0.013}_{-0.017}$
σ_{ELODIE}	RV jitter	$\rm km/s$	Log-uniform	0.007	$0.007\substack{+0.001\\-0.001}$
$\gamma_{\rm HIRES-POST}$	RV ZP	$\rm km/s$	Uniform	-0.0041	$-0.017\substack{+0.013\\-0.016}$
$\sigma_{ m HIRES-POST}$	RV jitter	$\rm km/s$	Log-uniform	0.0031	$0.0031\substack{+0.0002\\-0.0002}$
$\gamma_{\rm HIRES-PRE}$	RV ZP	$\rm km/s$	Uniform	0.0032	$-0.010^{+0.013}_{-0.017}$
$\sigma_{\mathrm{HIRES-PRE}}$	RV jitter	$\rm km/s$	Log-uniform	0.0027	$0.0028\substack{+0.0004\\-0.0004}$
$\gamma_{ m HRS}$	RV ZP	$\rm km/s$	Uniform	-0.032	$-0.045^{+0.013}_{-0.017}$
$\sigma_{ m HRS}$	RV jitter	$\rm km/s$	Log-uniform	3.9e-05	$0.00015\substack{+0.00084\\-0.00013}$
\mathcal{M}_{b}	Mass of b	M_{J}	Log-uniform $[0.2,20]$	9.2	$8.9^{+1.3}_{-1.7}$
\mathcal{M}_{c}	Mass of c	M_{\odot}	Log-uniform $[0.2,20]$	7.5	$7.9^{+1.6}_{-1.2}$
\mathcal{M}_{A}	Mass of A	M_{\odot}	$\mathcal{N}(0.98, 0.04)$	0.965	$0.97\substack{+0.04\\-0.04}$
Θ	Mutual inclination	degree		31.51	$32.09^{+13.75}_{-14.90}$
Θ *	Mutual inclination	degree		141.5	$145.0^{+16.04}_{-10.89}$

Table 1. Orbit fit results. The results of the longest MCMC run using orbitize! was adopted here. * $i_b < 90^\circ$ mode solutions for the orbit of b, with roughly 3 to 1 probability compared to the mode containing $i_b < 90^\circ$ solutions. [†] The argument of periastron of the planet's orbit, not the star's orbit, about the center of mass. [‡] Defined as $\tau = \frac{t_p - t_{ref}}{P}$, where t_p is the time of periastron passage and $t_{ref} = 58849.0$ MJD.

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C. ATMOSPHERIC MODELING

We compute custom atmospheric models using PICASO (N. E. Batalha et al. 2019; S. Mukherjee et al. 2023), an 491 open-source Python-based framework that solves for one-dimensional pressure-temperature (P-T) profiles in radia-492 tive-convective and chemical equilibrium. For cloud modeling, we adopt the EddySed framework outlined in (A. S. 493 Ackerman & M. S. Marley 2001), a method extensively used in previous studies (A. J. Skemer et al. 2016; C. V. 494 Morley et al. 2015), as well as in model grids such as those from (D. Saumon & M. S. Marley 2008) and the Sonora 495 Diamondback suite (C. V. Morley et al. 2024). Within PICASO, we incorporate an updated cloud treatment using 496 Virga (N. Batalha et al. 2020), a Python-based implementation of the (A. S. Ackerman & M. S. Marley 2001) model. 497 The mini-grid spans effective temperatures of $T_{\text{eff}} = [275, 300, 325 \text{ K}]$, surface gravity of $\log(g) = 4.25$ (cgs), eddy 498 diffusion parameter of $K_{zz} = [10^2, 10^7, 10^9 \text{ cm}^2 \text{ s}^{-1}]$, a metallicity of [M/H] = +0.5 (relative to the sun), and a solar 499 C/O ratio. Cloudy models have an $f_{sed} = 8$, with H_2O as the only condensing species. These models are part of 500 a larger grid that will be released in the future, extending the Sonora Bobcat (M. S. Marley et al. 2021a), Sonora 501 Diamondback (C. V. Morley et al. 2024), and Sonora Elf Owl (S. Mukherjee et al. 2024c). 502

Our custom models differ from the Sonora Elf Owl models in three key aspects of atmospheric chemistry. First, we adopt an updated treatment of CO_2 . Previous studies have shown that Sonora Elf Owl underestimates CO_2 abundances compared to JWST observations of cool substellar objects (S. A. Beiler et al. 2024b). To address this imbalance, we implement a CO_2 kinetic model based on the chemical kinetics described in (K. J. Zahnle & M. S. Marley 2014b),



Figure 9. Posterior distribution on the orbital elements of 14 Her b, from the orbitize! orbit fit. Two solutions for the planet's inclination i_b and longitude of the ascending node Ω_b arise due to the ambiguity of the direction of the planet's orbit.

⁵⁰⁷ following recent investigations into its impact (N. F. Wogan et al. 2023; S. Mukherjee et al. 2024a). This update leads ⁵⁰⁸ to a stronger CO₂ absorption feature near 4.2 μ m. Second, unlike Sonora Elf Owl, our models incorporate rainout ⁵⁰⁹ chemistry for condensates such as H₂O, even in cloud-free atmospheres, following the chemical rainout treatment in ⁵¹⁰ the Sonora Bobcat models. Finally, we exclude PH₃, as its abundance was found to be overestimated in Elf Owl ⁵¹¹ models compared to cool brown dwarf observations (S. A. Beiler et al. 2024b).



Figure 10. Posterior distribution on the orbital elements of 14 Her c, from the orbitize! orbit fit. Tails on the distributions are correlated with the rv instrumental jitter terms, due to the fractional phase coverage of the observations from various instruments. An additional epoch of JWST/NIRCam imaging will constrain these parameters dramatically by revising the planet's eccentricity estimate.

D. POTENTIAL FOR VON ZEIPEL-LIDOV-KOZAI OSCILLATIONS

The orbital structure of the 14 Her system suggests the possibility that the system might be experiencing von Zeipel-Lidov-Kozai (ZLK) oscillations, characterized by coupled high-amplitude eccentricity and inclination oscillations in misaligned, hierarchical three-body systems between the ZLK critical angles $39.2^{\circ} < \Theta < 140.8^{\circ}$. However, the very concept of ZLK is ill-defined for 14 Her-like systems. The prototypical ZLK effect is defined in the limit of a massless

test particle and a massive perturber on a circular orbit. The further a system strays from this regime, the more the system's secular evolution deviates from traditional ZLK behavior (S. Naoz 2016). In particular, the relatively equal planetary masses in the 14 Her system make classifying a particular system evolution as ZLK behavior not just difficult, but arguably meaningless. Regardless of the specific class of oscillation, we emphasize that the system at present is undoubtedly undergoing extreme mutual dynamical interactions.

About 30% of the inferred distribution of the mutual inclination Θ lies between the ZLK critical angles (H. von Zeipel 1910; M. L. Lidov 1962; Y. Kozai 1962). The ZLK mechanism is thought to have widespread consequences for planetary systems, including elongating the orbits of comets in our Solar System, as well as triggering high eccentricity migration of planets to become hot Jupiters (S. Naoz et al. 2011). While a number of extrasolar systems are believed to have experienced ZLK oscillations in the past (Y. Wu & N. Murray 2003), 14 Her is the first instance in which an ongoing ZLK mechanism may be observed on a mature system with long-period exoplanets.

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